

# **Introduction to Section Analysis and Design of Vehicle Structure Components**

**- For Crush Strength (Safety) and Stiffness (NVH)**

# Agenda

1. Technical background and beam theory review.
2. Section design for safety and stiffness (NVH).
3. Using CAE tools Section D – techniques, tips and demo.
4. Q & A.

# Background: Why Section Analysis/Design

- 1) Section reflect the characteristics of body structural components in
  - a) Stress (Durability/Fatigue). The major factors: material, size.
  - b) Stiffness (NVH). The major factors: size, shape, reinforcements.
  - c) Strength (Crash Safety). The major factors: material, size, shape.
  
- 2) Master sections are the base for vehicle structural construction.
  
- 3) Sections are 2D, which means
  - a) Straightforward, simple and quick to analyze, design and modify.
  - b) The analysis results are simplified, approximate and best for trend design purposes.

# Section Analysis Foundation and Limitation

- Section analysis is based on the beam theory therefore, can only be applied to beam-like components – pillars, roof rails and headers, front/rear rails and shotguns...
- Stiffness properties are based on linear beam theory.
- Crush strengths are based on the thin-wall buckling and nonlinear strength-hardening theory with experimental factors.
- Formulae are closed form enabling speedy computation.

# Beam Theory – Axial Loading

Axial crush strengths:

$$P_{cr} = \sigma_{cr} A$$

$$P_{max} = \sigma_{max} A$$

$P_{cr}$  and  $\sigma_{cr}$  are the force and stress at the elastic limit.

$P_{max}$  and  $\sigma_{max}$  are the force and stress at the failure.

$A$  is the section area that represents weight.

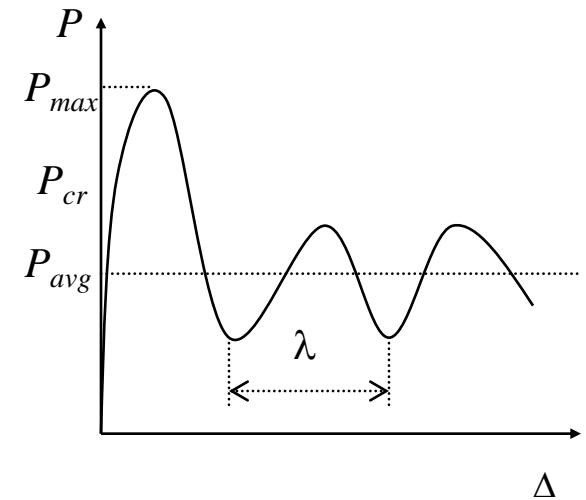
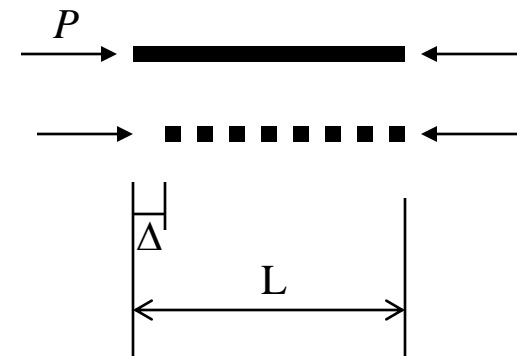
Axial deformation:

$$\Delta = \frac{PL}{EA}$$

$L$  is the beam length.

$A$  is the section area that represents axial stiffness.

$E$  is Young's modulus that represents material effect.



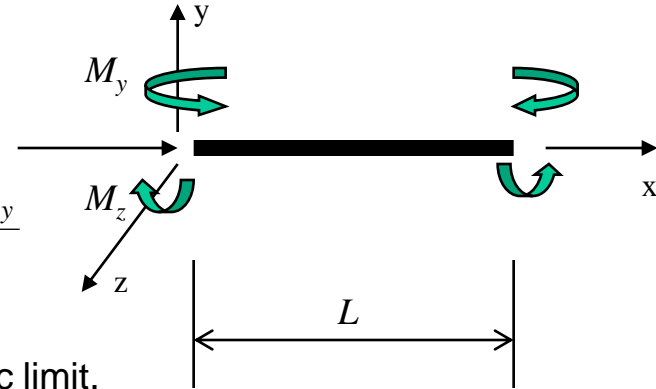
Buckling Force-Displ. Relationship

# Beam Theory – Bending

Bending crush strengths:

$$\sigma_{cr} = \frac{M_{cr-y} c_z}{I_y} + \frac{M_{cr-z} c_y}{I_z} \quad \sigma_{max} = \frac{M_{max-y} c_z}{I_y} + \frac{M_{max-z} c_y}{I_z}$$

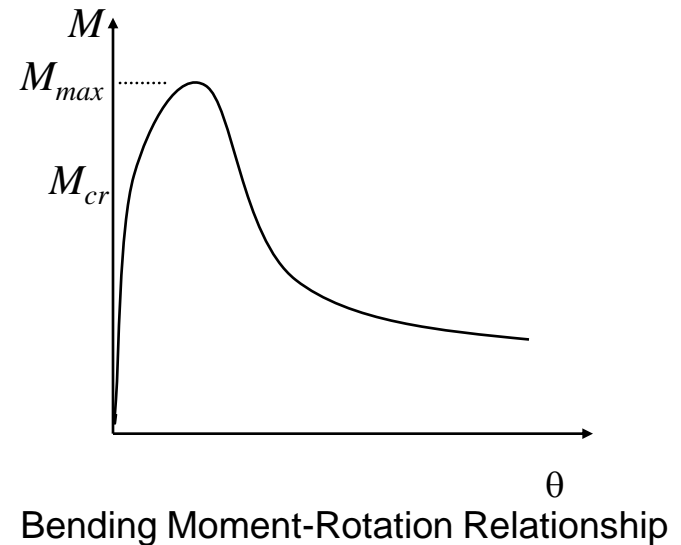
$M_{cr-y}$  and  $M_{cr-z}$  are bending moments about y and z axes at the elastic limit.  
 $M_{max-y}$  and  $M_{max-z}$  are bending moments about y and z axes at the failure.  
 $I_y$  and  $I_z$  are section moment inertia about y and z axes.



Bending deformation:

$$\theta_y = \frac{M_y L}{EI_y} \quad \theta_z = \frac{M_z L}{EI_z}$$

$I_y$  and  $I_z$  represent bending stiffness about y and z axes.

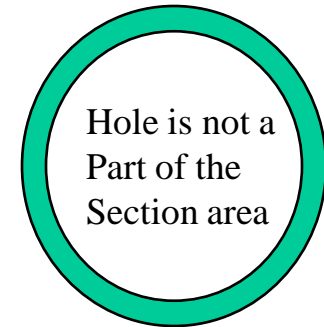


# Geometric Properties - Area

Section area:

$$A = \int_A dA$$

1. Proportional to the axial stiffness.
2. Affects the axial strength (crush load).
3. Represents component self-weight.



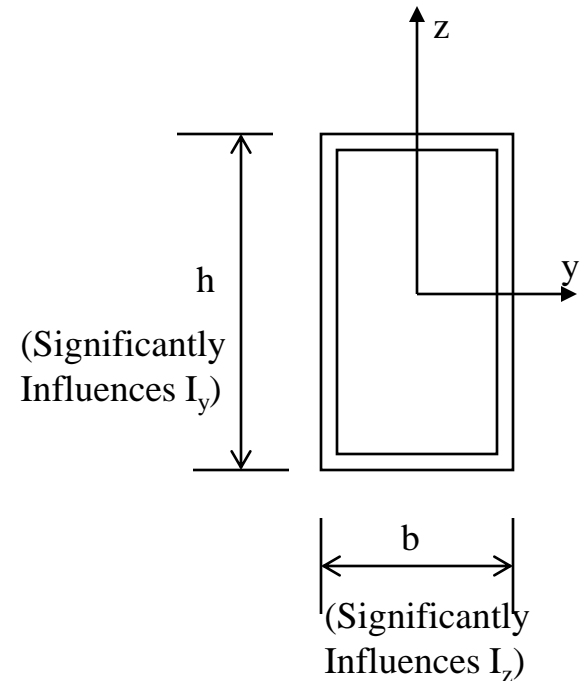
# Geometric Properties – Moment Inertia

Bending moments inertia:

$$I_y = \int_A z^2 dA$$

$$I_z = \int_A y^2 dA$$

1. Proportional to bending stiffness.
2. Proportional to bending strength.
3. Square relation ship with the section size.

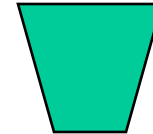




# Geometric Properties – Torsion Constant

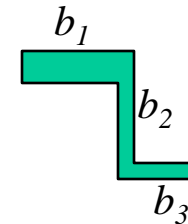
Solid section (ineffective with respect to weight):

$$J = \int_A r^2 dA$$



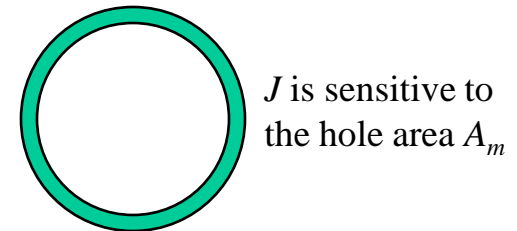
Thin-wall open section (weak torsion rigidity):

$$J = \sum \frac{1}{3} b t^3$$



Thin-wall closed section (strong and effective):

$$J = \frac{4A_m^2}{\oint \frac{ds}{t}}$$

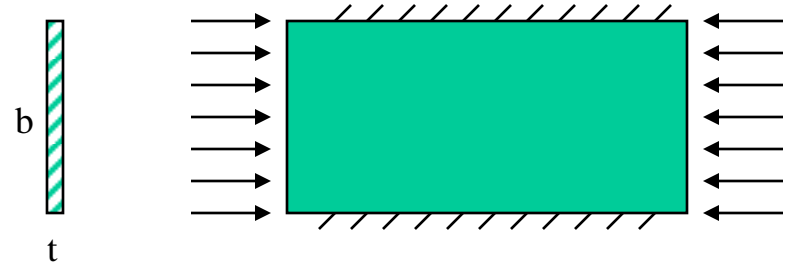


1. Proportional to the torsion stiffness.
2. Proportional to the torsion strength.

# Thin-Plate Buckling Stress - Theory

Based on the thin-wall buckling theory, a plate buckles at stress level:

$$\sigma_{cr} = k \frac{\pi E}{2(1 + \nu)} \left( \frac{t}{b} \right)^2$$



$k$  is the boundary support factor – shape factor

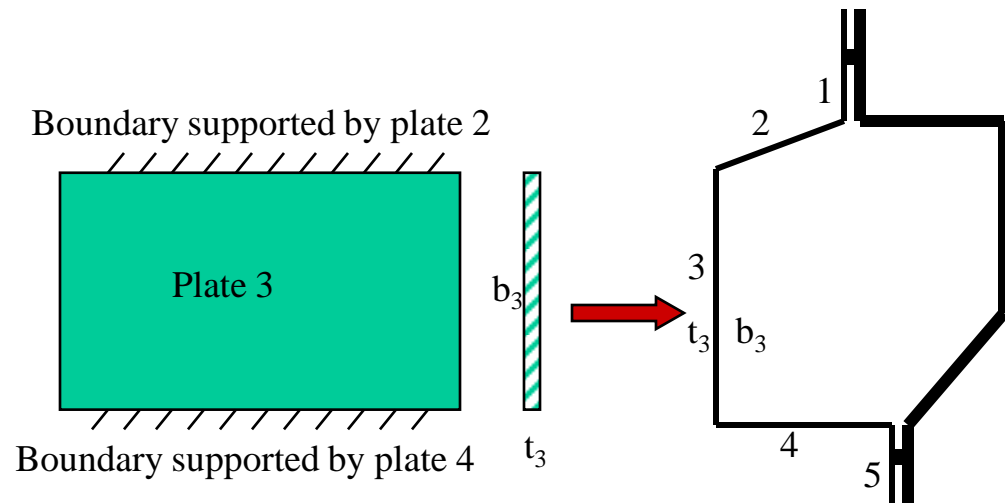
$\nu$  is poison's ratio,  $E$  is Young's modulus – material properties

$t$  is thickness,  $b$  is the width – geometric factors

# Section Strength = Buckling Strength of All Plates

- Automotive body components almost always fail in buckling.
- Section can be viewed as a combination of thin-wall plates (segments).

$$\sigma_{cr} = k \frac{\pi E}{2(1+\nu)} \left( \frac{t}{b} \right)^2$$



# Crush Property – Axial Strength

## Compression – buckling mode dominates

Upper limit:  $P_{\max} = \sum_{i=1}^n (\sigma_{cr})_i A_i$       -assume all segments reach buckling  
-weakest segment reaches buckling

Lower limit:  $P_{\max} = \sigma_{cr-\min} A$       -adopted in Section D2.0

where  $A_i$  is the area of segment  $i$  and  $A$  is the total area of the section.

## Tension – yielding mode governs

$$P_{\max} = \sigma_y A$$

# Crush Property – Bending Strengths

About y axis:  $M_{\max-y} = \frac{\sigma_{cr} I_y}{c_z}$  - Compression side buckles

About z axis:  $M_{\max-z} = \frac{\sigma_{cr} I_z}{c_y}$  - Compression side buckles

The above equations are based on symmetric sections ( $I_{yz}=0$ ) and are for demonstration purpose. The equations are more complex for general shape of sections.

# Crush Property – Summary

In NVH and durability design look for 5 geometric properties:

$A$ ,  $I_y$ ,  $I_{yz}$ ,  $I_z$  and  $J$

For safety considerations, look for 5 crush strengths:

$P_{max}$ ,  $M_{max-y}$ ,  $M_{max-z}$ , and  $M_{max+y}$ ,  $M_{max+z}$

# Section Design and Optimization

Property	Action	Results	Effective Means
$A$	decrease	light weight	reduce thickness, section size, use high-strength material.
$I_y$ and $I_z$	increase	high stiffness	increase size; move material far away from center.
$J$	increase	high stiffness	adopt closed section.
$P_{max}$	increase	strong crush strength	increase thickness, reduce size, add corners, reinforcements.
$M_{max}$	increase	strong crush strength	increase thickness and add corners, reinforcements on compression side.

# Conflict Between Safety and NVH

**NVH Objectives:**  
Maximize  $I_y$ ,  $I_z$  and  $J$ , Minimize  $A$

$$I_y = \int_A z^2 dA$$

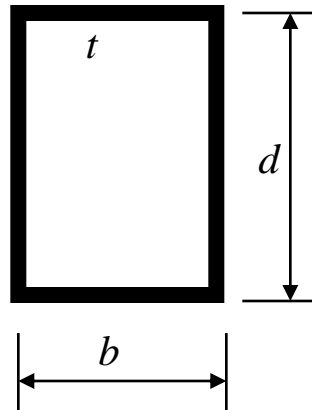
$$I_z = \int_A y^2 dA$$

$$A = \sum bt + \sum dt$$

Maximize  $I_y$  and  $I_z$   
Minimize  $A$

Maximize  $b$  and  $d$   
Minimize  $t$

**Fight**



**Fight**

**Safety Objectives:**  
Maximize  $P_{max}$ ,  $M_{max-y}$ ,  $M_{max-z}$

$$\sigma_{cr} = k \frac{\pi E}{2(1+\nu)} \left(\frac{t}{b}\right)^2$$

$$P_{max} = \sigma_{cr} (\sum tb + \sum td)$$

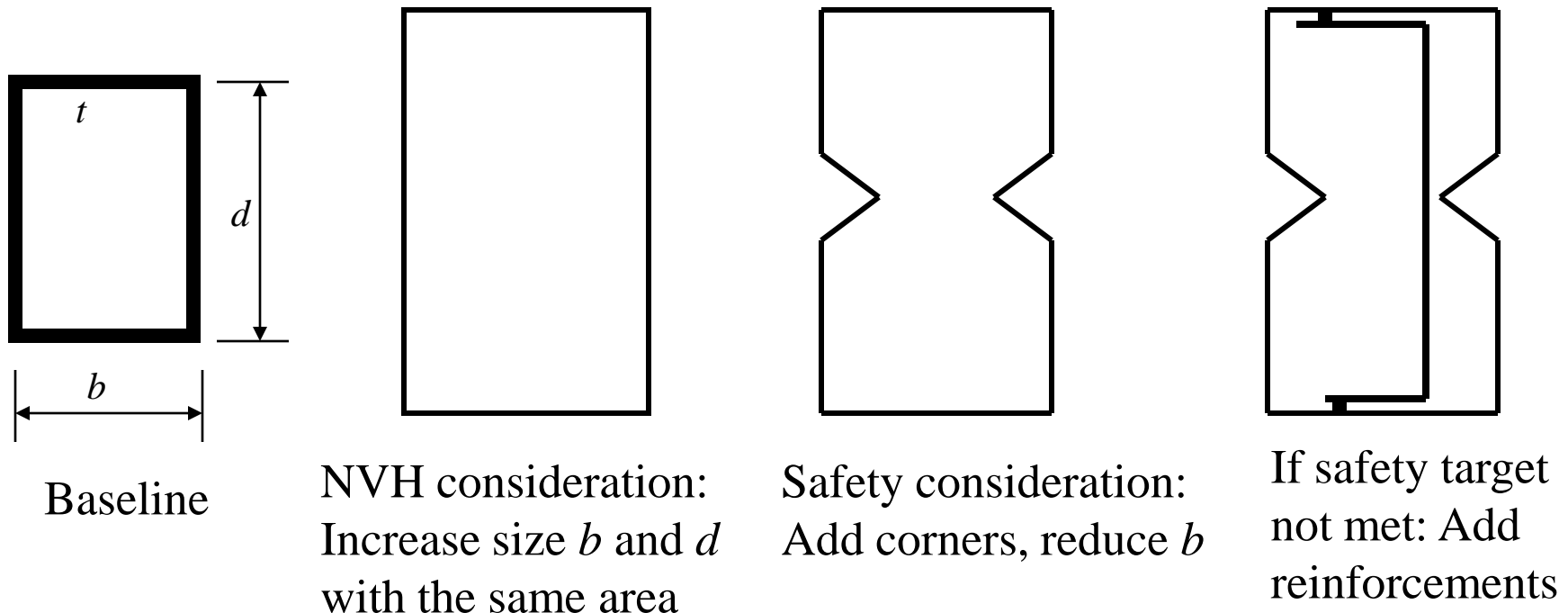
Maximize  $P_{max}$   
Minimize  $\sigma_{cr}$

Minimize  $b$  and  $d$   
Maximize  $t$



# Section Design for Both Safety and NVH

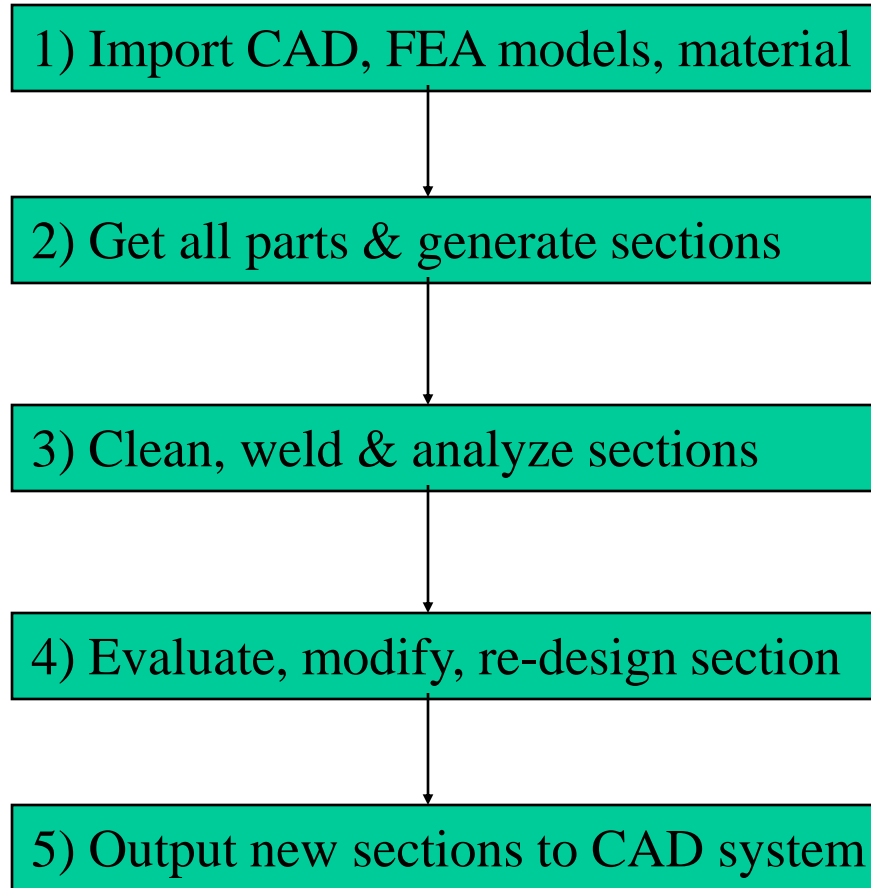
- 1) Use maximum space allowed for section to maximize stiffness  $I_y$ ,  $I_z$ .
- 2) Reduce thickness as much as possible to minimize weight  $A$ .
- 3) Add corners on compressed plates to maximize crush strengths  $P_{max}$ ,  $M_{max}$ .
- 4) Add reinforcements if adding corners can not meet crush requirements.



## Section D 4.0 Major New Features

1. Compatible with Dyna3D, Radioss (Fix and Block Format) Inputs
  - Large models up to 1 million elements.
2. Section Part Sensitivity/Optimization:
  - Sensitivity to part thickness.
  - Sensitivity to part weight.
  - Part optimization.
3. Section Analysis Under Combined Loads:
  - Stress at any load combination.
  - Buckling & ultimate levels.
  - Failure segment prediction.
4. Baked-in Material Database (Mild, HSLA, DP & Boron steels!)
5. Improved Section Design/Modification Functions:
  - On-screen modifying thickness, material and part ID.
  - Complete tables listing material, part properties & elements.
  - Hypermesh-like view handling (dynamic zoom, rotation...)

# Section Design/Analysis – General Process



FEA models: Nastran, Radioss, Ideas.  
CAD data: Ideas surface, lines. PDGS lines.

Cut sections: FEA models, CAD lines.  
Sketch sections: directly draw, copy-paste.

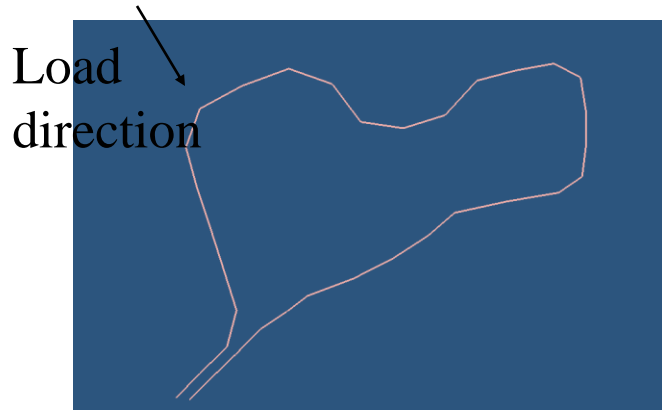
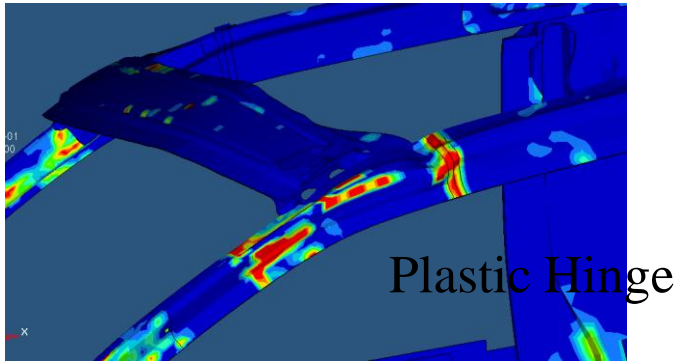
Weld all parts, check material properties.  
Get geometric properties I, J, A....  
Get crush strengths Pmax, Mmax...

Modify or re-design sections to meet objective.  
Means: shape, materials and reinforcement.

Save files in Section D or database formats.  
Print section analysis results and new shapes.  
Convert, output new sections to CAD system.

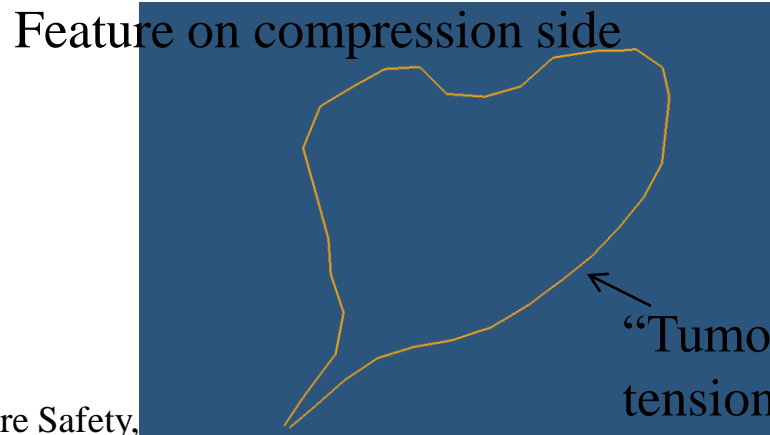
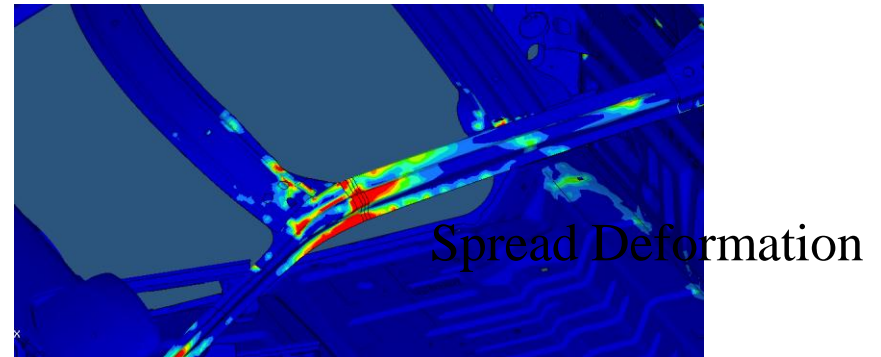
# Example-P415 Roof Rail Tube Section Design

Initial CAD section design resulted concentrated plastic hinge, undesirable mode and significantly lower roof strength.



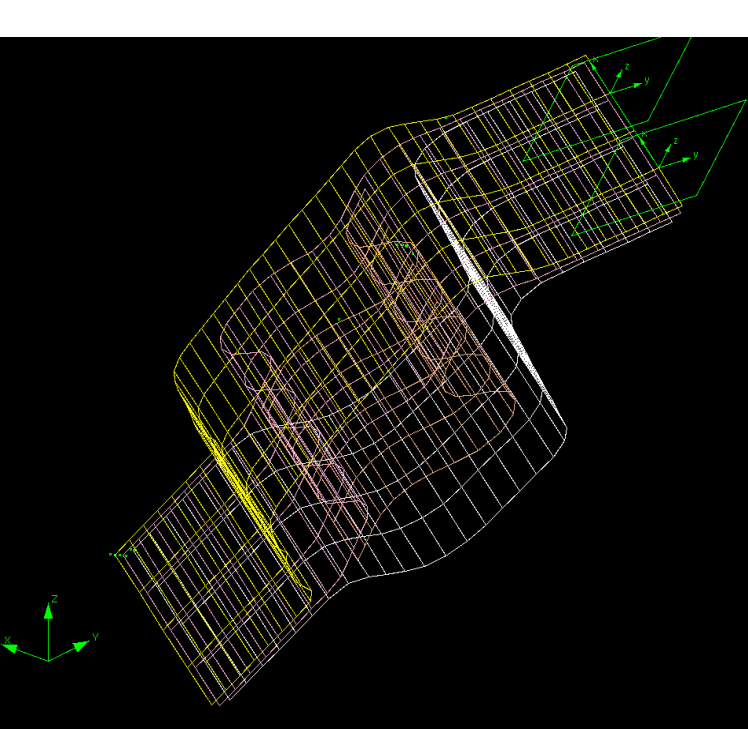
2016-06-25

After several iteration of section analysis "tumor is added to increase I value by 20% + in the loading direction and maintain compression feature for buckling strength.



Core Safety,

# DEMO



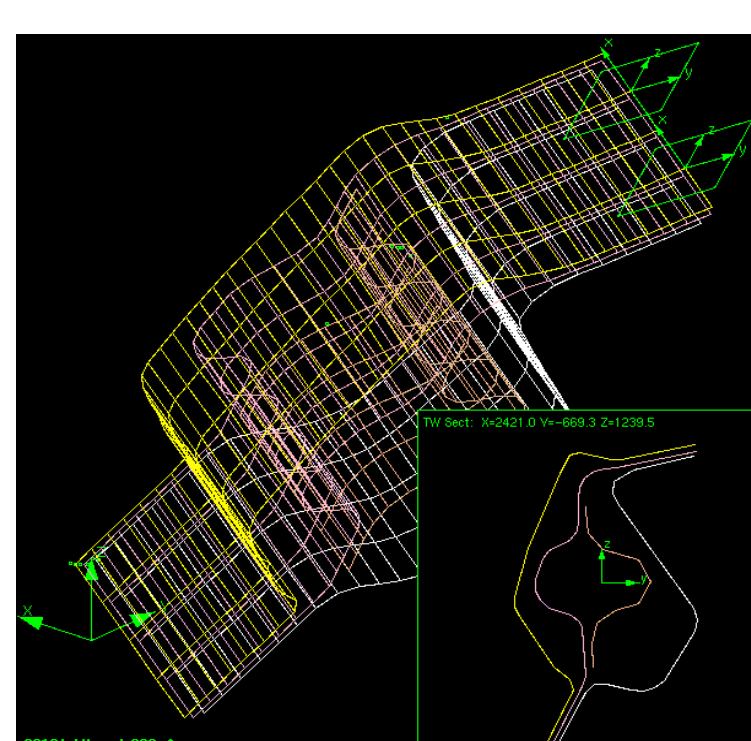
**Cutter/Local Coord.**  
 Cut Sections  
 Part & Property  
 Node/Point  
 Split/Combine/Find  
 Rotate/Zoom/MemView  
 Display Funtions  
 On/Off Display  
 Measure/Calculate  
 Create Element/Line  
 Copy/Delete Elm/Line  
 Check Model  
 Contact Surface  
 Check Elem Quality  
 SPC/Mass/Force/Vel  
 Connectivities  
 Define Component

XView YView ZView  
 Ry-90 Rz-90 45View  
 Undo Print Reset  
 Return Plot FitWin

**Crt/Del section cutter**  
 Modify section cutter  
 Crt/Del local coordinate  
 Modify local coordinate

node -> x (y/z/XY)  
 node -> x (3 nodes)  
 global axis -> x  
 line: nodes define x  
 node+angles x^X, x^Y  
 node+angles x^Y, x^X  
 node+angles x^Z, x^X  
 coordinate -> plane  
 delete a plane/coord.  
 del all planes/coord.

e0312/ai/dtang/try.gif  
 Mon May 5 15:23:58 ED



**Cutter/Local Coord.**  
 Cut Sections  
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 Contact Surface  
 Check Elem Quality  
 SPC/Mass/Force/Vel  
 Connectivities  
 Define Component

XView YView ZView  
 Ry-90 Rz-90 45View  
 Undo Print Reset  
 Return Plot FitWin

Section # 1  
 # of Sections 2  
 @ equal intervals  
 Weld automatically  
 Filter sect. nodes  
 Cut t-w section only

box select elements  
 polygon select...  
 select all elements  
 segment angle 6.00  
 length/thick. 2.00

TW Sect: X=2421.0 Y=-669.3 Z=1239.5  
 e0312/ai/dtang/x202\_A\_sec.nas

# Section Analysis – Clean, Weld Parts

X=2421.0 Y=-669.3 Z=1239.5

2 X=2429.2 Y=-667.5 Z=1245.0

- Show Thickness
- Show Node ID
- Show Segment ID
- Cell (loop)
- Principal Axes
- Shear Center
- 360 Mom. Inertia
- Round Corners
- Segment Arrows
- Uniform Scale
- Beam Reference
- Color by Part
- Compare Section
- Analyze Section
- Section -> Line
- Paste a Section
- Delete Section
- Replace Section
- Copy a Section
- Combine Section
- Grids
- Scroll
- Resequence IDs
- Undo all Change
- Del. Free Sect.
- Print
- Summary
- Return

/ae0312/utdang/x202\_A\_sec.nas

Tue May 6 09:11:42 EDT 2003

SECTION CRUSH STRENGTHS 1 X=2421.0 Y=-669.3 Z=1239.5

79. 42. 14. 16.4 31.3 46.2

1159. 1124. 368. 6.1 2.0

430. 449. 129. 95°

- Show Thickness
- Show Nodal #
- Show Segment #
- Show Cells
- Principal Axes
- Shear Center
- 360deg. Inertia
- Round Corners
- Segment Arrows
- Show Grids
- Node Coordinate
- Color by Part
- Forc-Disp Curve
- Move View Part
- Center View
- Box Zoom View
- Fit Screen View
- Analyze Stress
- Modify Node x,y
- Modify Property
- Modify Segment
- Modify Section
- Section Summary
- Plot
- Print
- Return
- Modify node
- Modify segment
- Resequence
- On/off display
- Coinside node/se
- Part options...
- Weld options...
- Rotate & flip
- Save/Undo/Comp..
- Return
- strike-through weld
- point-to-point weld
- delete a weld
- delete all welds
- miniz.all weld dist.

# Section Analysis – Read and Print Results

## SECTION CRUSH STRENGTHS

1 X=2421.0 Y=-669.3 Z=1239.5

**Axial Loading:** Shear @ Y:  
 Pcri= 78.07423 Vcriy= 7.86928  
 Pmax= 79.43654 Vmaxy= 9.83659  
 Pmin= 14.05728 Vminy= 4.91830  
 Pavg= 28.11455

**Torsion Twist:** Shear @ Z:  
 Tcri= 364.55 Vcriz= 27.28424  
 Tmax= 455.69 Vmaxz= 34.10530  
 Tmin= 227.84 Vminz= 17.05265

**Bending @ Y:** Bending @ Z:  
 Mcri+= 927.10 Mcri+= 359.11  
 Mmax+= 1158.88 Mmax+= 430.29  
 Mmin+= 368.26 Mmin+= 128.72

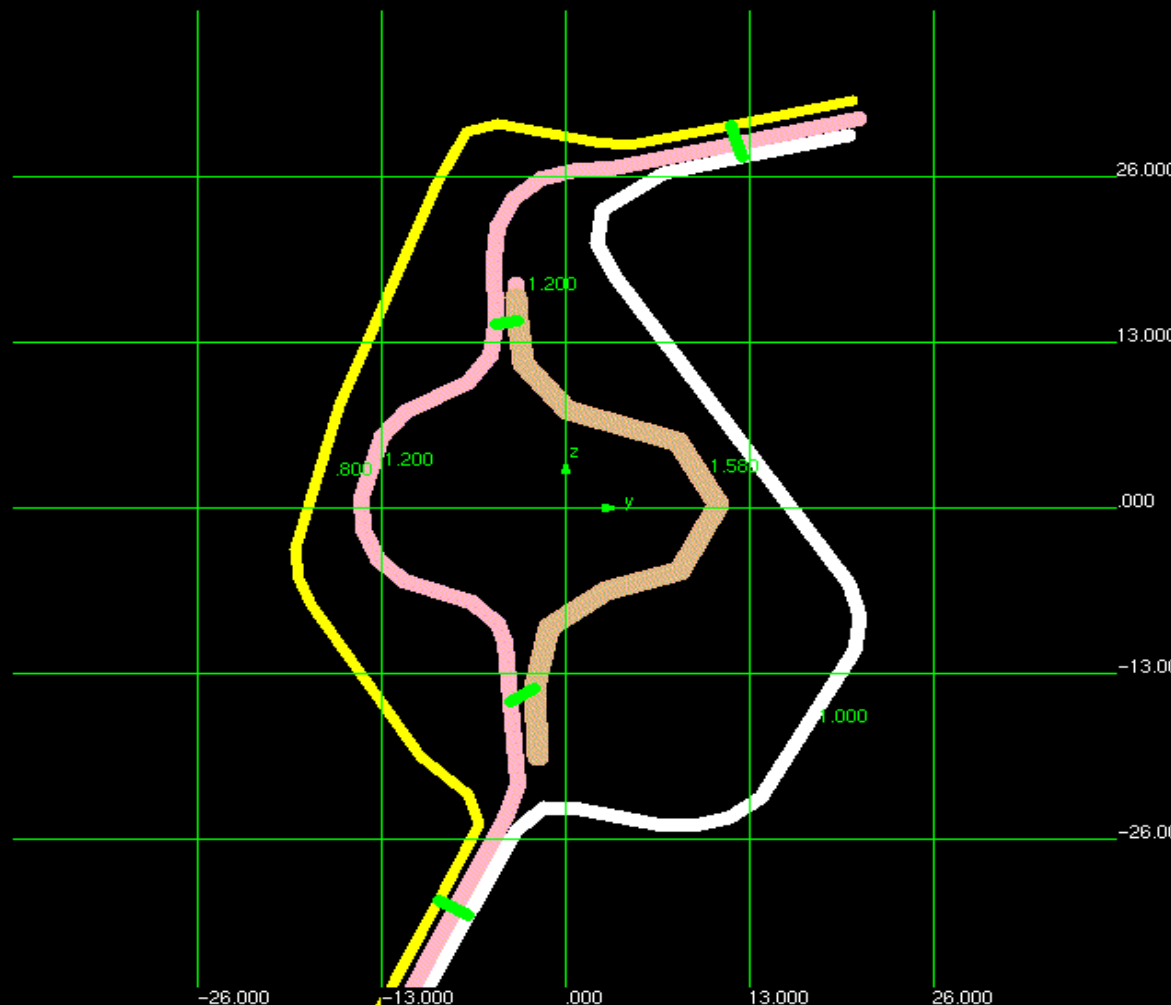
Mcri-= 937.43 Mcri-= 358.87  
 Mmax-= 1124.18 Mmax-= 448.58  
 Mmin-= 244.00 Mmin-= 95.04964

## EFFECTIVE PROPERTIES

Eff. Crush Area A = 377.32  
 Crush Moment Inertia Iy = 163288.  
 Crush Moment Inertia Iz = 41436.55

## GEOMETRIC PROPERTIES

A = 393.36 CGy = .00003  
 Iy = 163288. CGz = .00004  
 Iz = 41436.55 SCy = -2.12620  
 Iyz = 24452.77 SCz = 2.47216  
 J = 49721.82 ry = 20.374  
 Asy = 53.16879 rz = 10.264  
 Asz = 634.03 Wn = 321766.  
 Imax = 168012. Jo = 178.74  
 Imin = 36712.59 Zy = 4073.87  
 alph = -10.93410 Zz = 1989.37



Show Thickness

Show Nodal #

Show Segment #

Show Cells

Principal Axes

Shear Center

360deg. Inertia

Round Corners

Segment Arrows

Show Grids

Node Coordinate

Color by Part

Forc-Disp Curve

Move View Port

Center View

Box Zoom View

Fit Screen View

Analyze Stress

Modify Node x,y

Modify Property

Modify Segment

Modify Section

Section Summary

Plot

Print

Return

# Modification – Shape, Material/Thickness, Reinforcement

## SECTION CRUSH STRENGTHS

1 X=2421.0 Y=-669.3 Z=1239.5

### Axial Loading: Shear @ Y:

Pcrl= 87.42401 Vcrl= 56.79824  
 Pmax= 88.94946 Vmaxy= 70.99780  
 Pmin= 15.74071 Vminy= 35.49890  
 Pavg= 31.48141

### Torsion Twist: Shear @ Z:

Tcrl= 483.68 Vcrlz= 72.89790  
 Tmax= 604.60 Vmaxz= 91.12237  
 Tmin= 302.30 Vminz= 45.56118

### Bending @ Y: Bending @ Z:

Mcri+= 1120.92 Mcri+= 526.72  
 Mmax+= 1401.15 Mmax+= 652.04  
 Mmin+= 560.13 Mmin+= 195.37

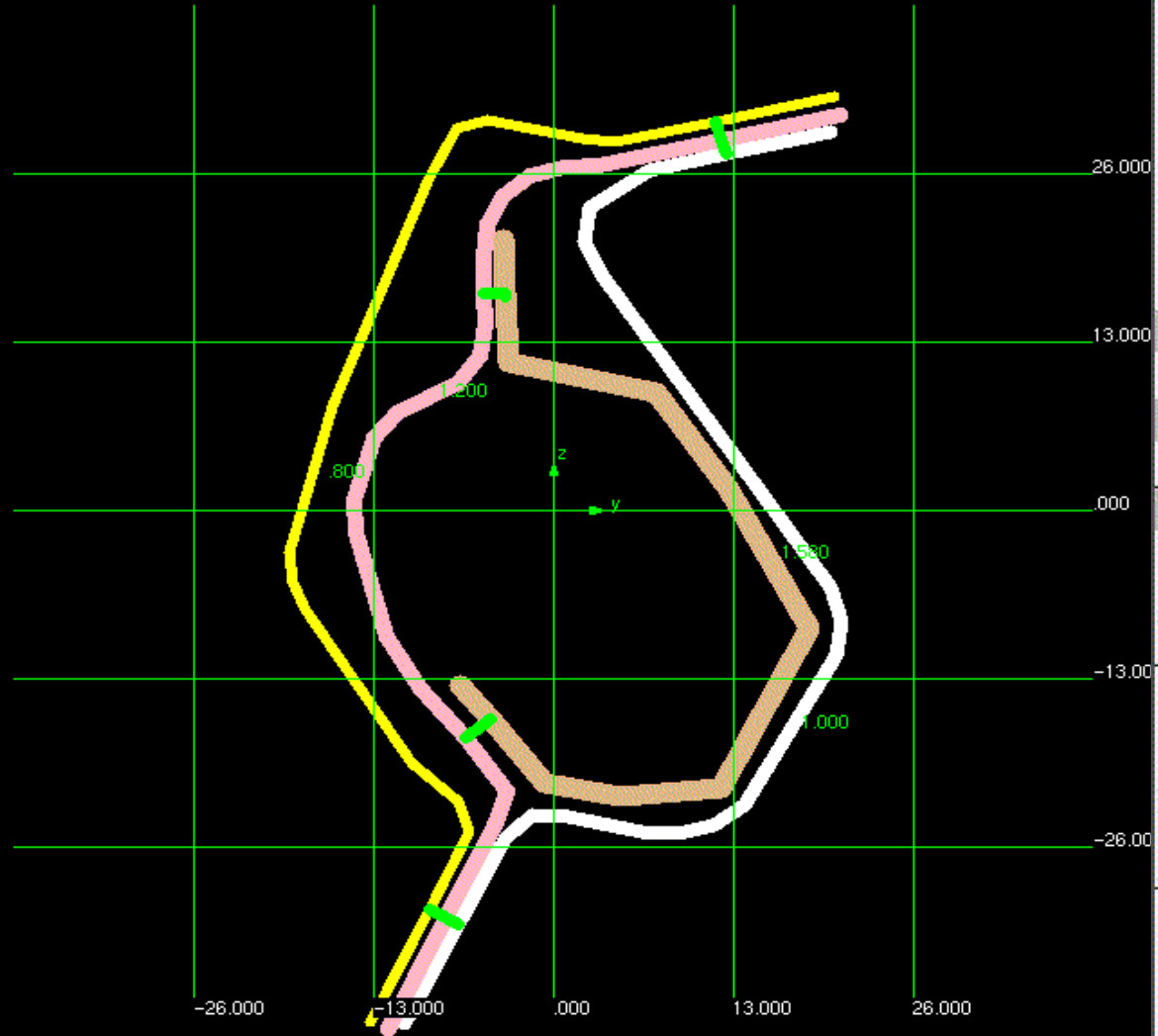
Mcri-= 1124.03 Mcri-= 524.56  
 Mmax-= 1313.47 Mmax-= 583.13  
 Mmin-= 317.84 Mmin-= 125.46

## EFFECTIVE PROPERTIES

Eff. Crush Area A = 423.09  
 Crush Moment Inertia Iy = 184704.  
 Crush Moment Inertia Iz = 52608.35

## GEOMETRIC PROPERTIES

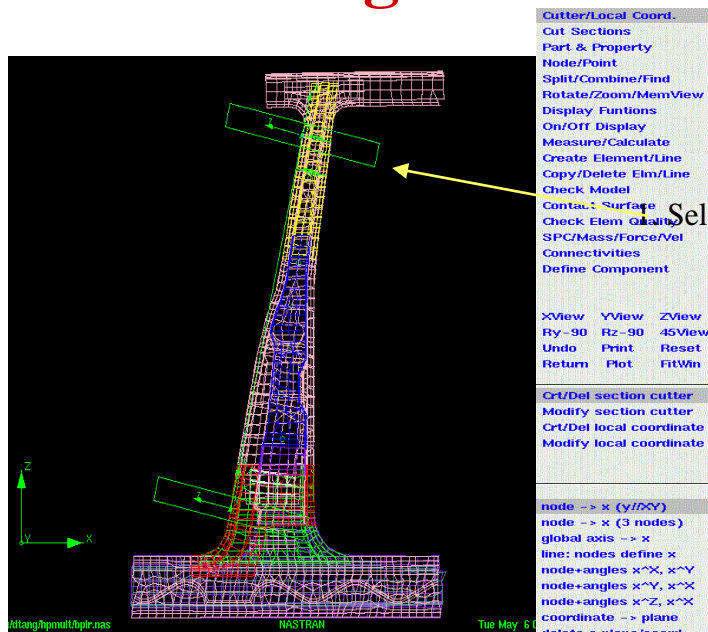
A = 440.46 CGy = 1.21409  
 Iy = 184704. CGz = -1.02580  
 Iz = 52608.35 SCy = .93462  
 Iyz = 18114.19 SCz = -.38244  
 J = 70923.31 ry = 20.478  
 Asy = 837.63 rz = 10.929  
 Asz = 7790.55 Wn = 383234.  
 Imax = 187143. Jo = 219.33  
 Imin = 50169.41 Zy = 4729.21  
 alph = -7.66837 Zz = 2592.48



- Show Thickness
- Show Nodal #
- Show Segment #
- Show Cells
- Principal Axes
- Shear Center
- 360deg. Inertia
- Round Corners
- Segment Arrows
- Show Grids
- Node Coordinate
- Color by Part
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- Move View Port
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- Fit Screen View
- Analyze Stress
- Modify Node x,y
- Modify Property
- Modify Segment
- Modify Section
- Section Summary
- Section Summary
- Plot
- Print
- Return

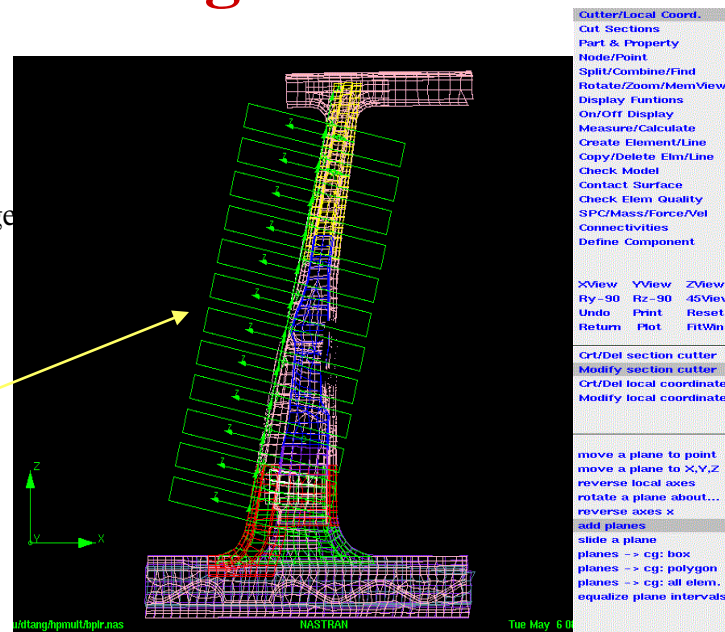


# Cutting Sections – Multiple Cutting Planes

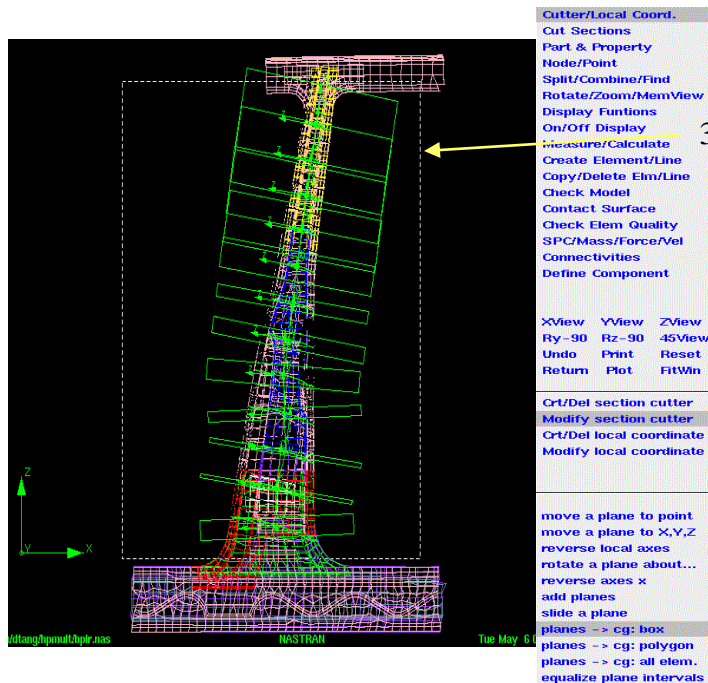


Select 2 points to specify range

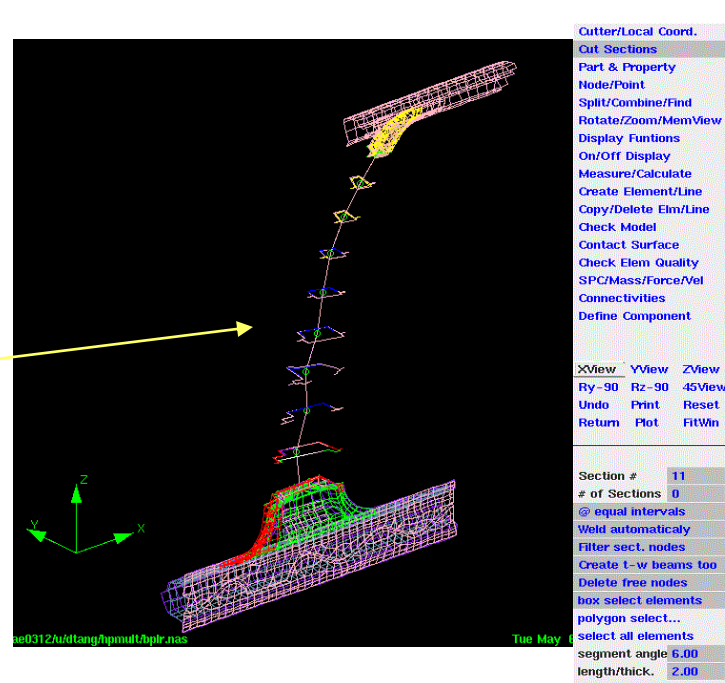
2. Add planes



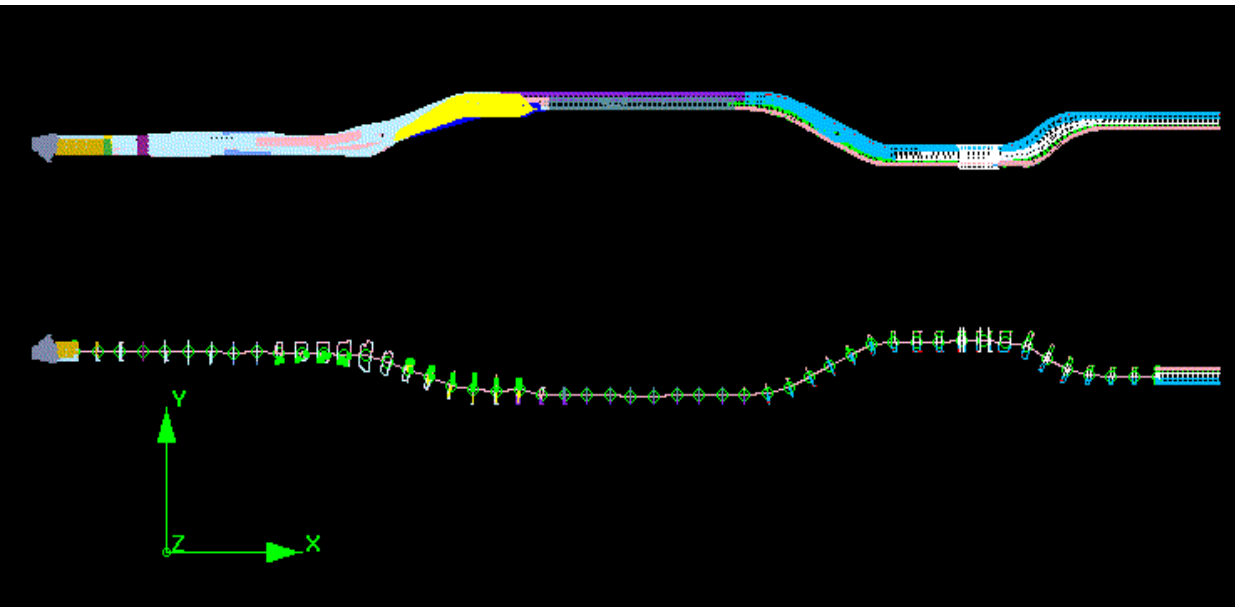
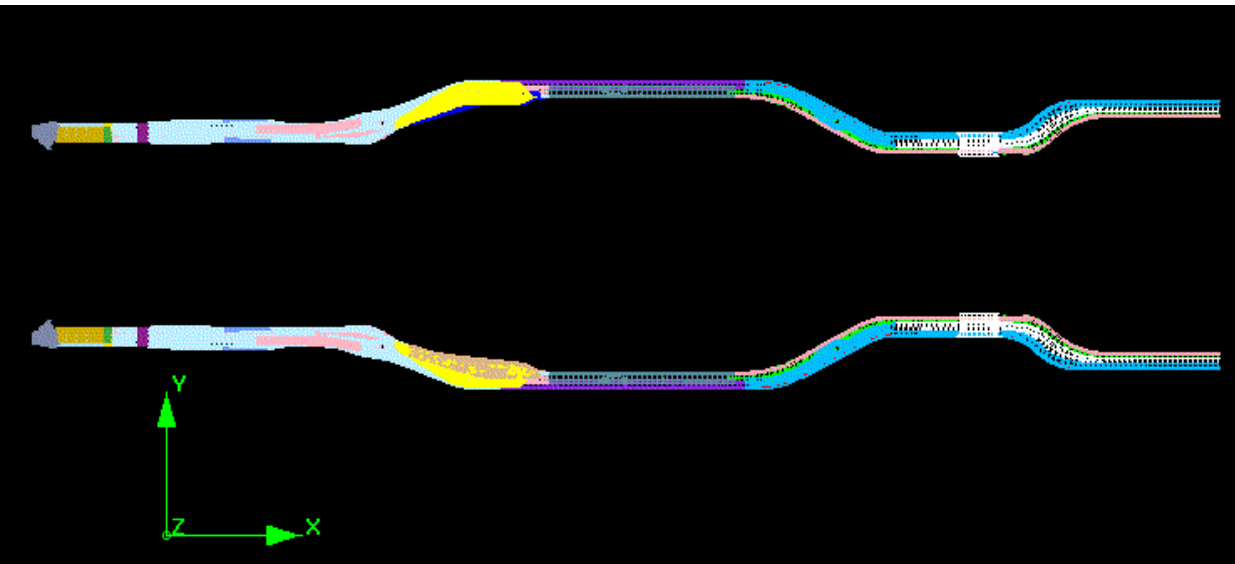
3. Move planes to CG



4. Cut sections

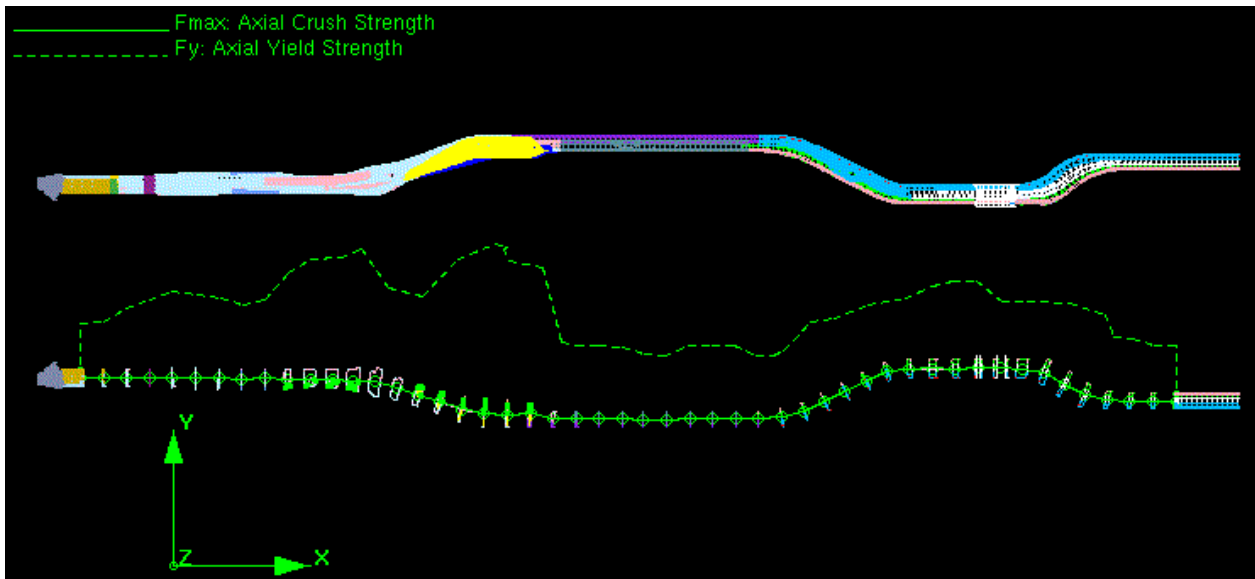
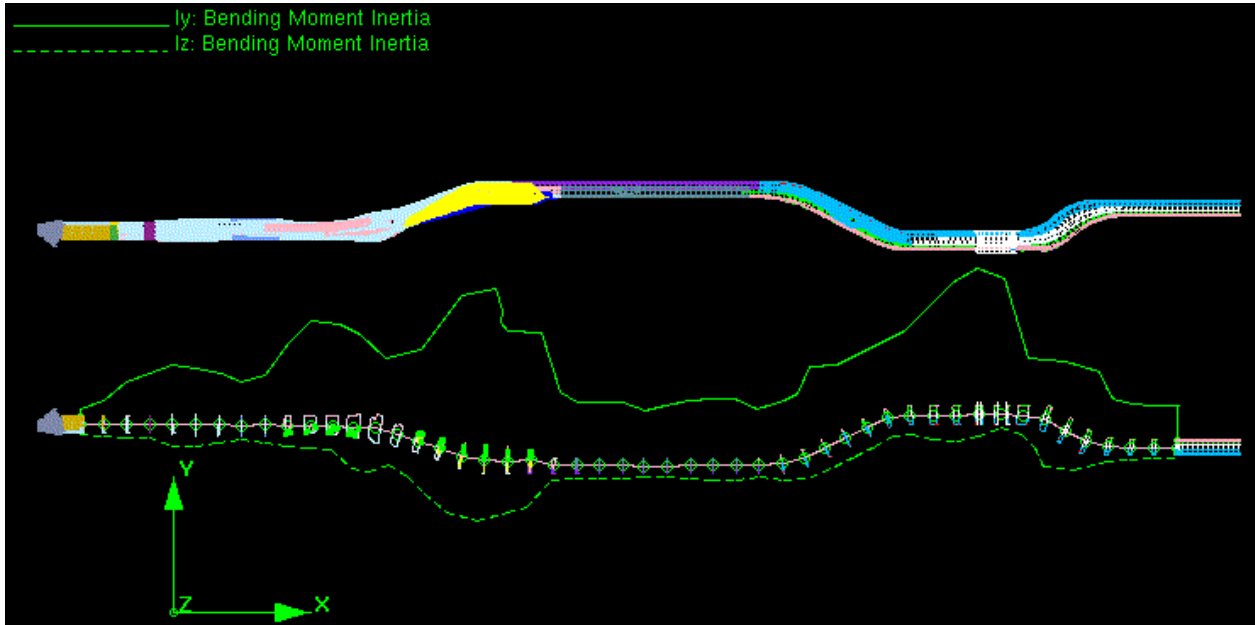


# Component Analysis- Cut Section & Create Beams



- Cutter/Local Coord.
  - Cut Sections
  - Part & Property
  - Node/Point
  - Split/Combine/Find
  - Rotate/Zoom/MemView
  - Display Functions
  - On/Off Display
  - Measure/Calculate
  - Create Element/Line
  - Copy/Delete Elm/Line
  - Check Model
  - Contact Surface
  - Check Elem Quality
  - SPC/Mass/Force/Vel
  - Connectivities
  - Define Component
- 
- |        |       |        |
|--------|-------|--------|
| XView  | YView | ZView  |
| Ry-90  | Rz-90 | 45View |
| Undo   | Print | Reset  |
| Return | Plot  | FitWin |

# Component Analysis- Display Component Performance



Cutter/Local Coord.  
 Cut Sections  
 Part & Property  
 Node/Point  
 Split/Combine/Find  
 Rotate/Zoom/MemView  
**Display Functions**  
 On/Off Display  
 Measure/Calculate  
 Create Element/Line  
 Copy/Delete Elm/Line  
 Check Model  
 Contact Surface  
 Check Elem Quality  
 SPC/Mass/Force/Vel  
 Connectivities  
 Define Component

XView YView ZView  
 Ry -90 Rz -90 45View  
 Undo Print Reset  
 Return Plot FitWin

Display modes  
 Options  
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2016-06-25

## When Section Analysis Adds Values....

1. New program - When design targets are set, sketch or modify a similar section to meet the requirements
2. Quick assessment for a design change – Find the implications for crush strength.
3. Design a reinforcement to meet an increased target or as a remedy for strength gap.
4. Use of high-strength or light-weight materials – Find the equivalent section size, thickness or shape to deliver the same performance.
5. Assess the load path – Use the component profile to make sure the desired strength distribution along the component (rail, pillar...).
6. ....

## Section D User Tips

- 1) If section is open and very stiff and later closed with weak segment using Section D, the overall section strength will be much much smaller than the open section as Section D considers section fails when the weak segment fails. In this case use only open section to compute its strength.
- 2) Use your judgment in how to use  $P_{cr}$ ,  $P_{avg}$  or  $P_{max}$  but it is recommended to use  $P_{avg}$  in case of side rails where crush is axial and  $P_{max}$  when crush is bending such as B pillar.
- 3) Use rails/pillars etc. without reinforcements when the capacity of structure is needed so that minimum load capacity is measured to be used for path load.
- 4) Make sure that the correct material and thickness is used when creating new segments in Section D. In this case a new material has to be created in Section D for the new created segments.
- 5) Section D that is installed now in our server is not the latest version to read Radioss ver. 4.1. It is in process to install the latest version. For now, Modedit can be used to read Radioss file and output Nastran file so that Section D can read it with no material or property lost.

# New Developments

## 1) Component Profile Feature:

- Maximum axial crush strength (Load path design)
- Average crush strength (Energy absorption)
- Bending crush strength (B pillar design for side impact)
- Geometric properties (Bending stiffness, weight...)

## 2) Combined Axial and Bending loads

- Strength reduction due to offset
- Failure surface

## 3) Mixed High and Low Strength Materials

- DP600, DP780, DP980, Martensite, Boron steels
- Aluminum 5754, 6111...

## 4) New User Manual 2.0 & Section D Hands on Training.